

# Bringing Causality into Fairness: Application to Pretrial Public Safety Assessment

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Randomization, Neutrality, and Fairness

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# Fairness, Decision-Making, and Causality

- Fairness of decision-making must consider the **impact** of decision
  - admissions, hiring, insurance, lending, medical treatment, etc.
  - public policies: court decisions, government funding and programs, etc.
- We must account for how decisions influence individuals
- In contrast, the literature on algorithmic fairness focuses on **prediction**
- Fundamental difference between **causation and association**
- In this talk, I will:
  - 1 introduce statistical fairness criteria based on causality
  - 2 compare them with standard statistical fairness criteria
  - 3 apply them to the unique field experiment in criminal justice

# Statistical Fairness Criteria

- Originally developed for assessing the fairness of prediction algorithms
- But also used for assessing the fairness of algorithmic/human decision
- Setup:
  - outcome:  $Y$
  - prediction or decision:  $D$
  - protected attribute (e.g., race, gender):  $A$
- Three statistical fairness criteria:
  - 1 equal prediction/decision:  $D \perp\!\!\!\perp A$
  - 2 equal accuracy:  $D \perp\!\!\!\perp A \mid Y$
  - 3 equal calibration:  $Y \perp\!\!\!\perp A \mid D$

# Principal Fairness: Taking Causality into Account

- The statistical fairness criteria ignore the fact that the decision may **affect** the outcome
  - ① fairness should address how individuals are affected by the decision
  - ② observed data are contaminated (related to **selective labels problem**)
- Causality framework:
  - binary decision:  $D$
  - potential outcomes:  $Y(1)$  and  $Y(0)$
  - different from the observed outcome:  $Y = Y(D)$
  - causal effect:  $Y(1) - Y(0)$
  - fundamental problem of causal inference
  - **principal strata**:  $R = (Y(1), Y(0)) = (y_1, y_0)$
- **Principal fairness**:
  - accuracy:  $D \perp\!\!\!\perp A \mid R$  individuals who are similarly affected by the decision should be treated similarly
  - calibration:  $R \perp\!\!\!\perp A \mid D$  individuals who receive a similar decision should behave similarly

# An Illustrative Example

Group A		$Y(0) = 1$	$Y(0) = 0$
		Dangerous	Backlash
$Y(1) = 1$	Detained ( $D = 1$ )	120	30
	Released ( $D = 0$ )	30	30
		Preventable	Safe
$Y(1) = 0$	Detained ( $D = 1$ )	70	30
	Released ( $D = 0$ )	70	120
Group B		$Y(0) = 1$	$Y(0) = 0$
		Dangerous	Backlash
$Y(1) = 1$	Detained ( $D = 1$ )	80	20
	Released ( $D = 0$ )	20	20
		Preventable	Safe
$Y(1) = 0$	Detained ( $D = 1$ )	80	40
	Released ( $D = 0$ )	80	160

- Satisfies principal fairness in terms of accuracy (but not calibration)
  - “Dangerous” group ( $y_0 = 1, y_1 = 1$ ): 80%
  - “Safe” group ( $y_0 = 0, y_1 = 0$ ): 20%
  - “Preventable” group ( $y_0 = 1, y_1 = 0$ ): 50%
  - “Backlash” group ( $y_0 = 0, y_1 = 1$ ): 50%

## The Same Example Does Not Satisfy Statistical Fairness

	Group A		Group B	
	Detained	Released	Detained	Released
$Y = 1$	150	100	100	100
$Y = 0$	100	150	120	180

- This observed data are consistent with the previous example
- Statistical fairness in terms of accuracy (and calibration) is not satisfied
  - Group A: 60% ( $Y = 1$ ), 60% ( $Y = 0$ )
  - Group B: 50% ( $Y = 1$ ), 40% ( $Y = 0$ )

# Relations between Principal Fairness and Statistical Fairness

## Theorem 1

- 1 If  $A \perp\!\!\!\perp R$  holds, principal fairness implies all three statistical fairness criteria
- 2 If  $A \perp\!\!\!\perp R$  and  $Y(1) \leq Y(0)$  (i.e., monotonicity) hold, principal fairness is equivalent to the three statistical fairness criteria

- $A \perp\!\!\!\perp R$  is the **equal base rate** condition with potential outcomes
- The results hold conditional on covariates
- Monotonicity eliminates the “Backlash” group in our example

# Empirical Evaluation and Policy Learning

- Difficulty: principal strata are unobserved
  - ① partial identification
  - ② unconfoundedness assumption:

$$Y(d) \perp\!\!\!\perp D \mid X \quad \text{for any } d$$

where  $X$  is the decision variables

- Unconfoundedness is plausible if  $X$  is known and observed
- Under monotonicity and unconfoundedness, we can identify **principal score**:  $e_r(X, A) = \Pr(R = r \mid X, A)$
- **Policy evaluation**: compute  $\Pr(D = 1 \mid R, A)$
- **Policy learning**:
  - decision rule:  $D = \delta(X)$
  - $\Pr(\delta(X) = 1 \mid R = r, A) = \mathbb{E} \left[ \frac{e_r(X, A)}{\mathbb{E}\{e_r(X, A) \mid A\}} \delta(X) \mid A \right]$
  - optimal policy subject to the fairness constraint



# Pretrial Public Safety Assessment (PSA)

- Algorithmic recommendations often used in US criminal justice system
- At the **first appearance hearing**, judges primarily make two decisions
  - ① whether to release an arrestee pending disposition of criminal charges
  - ② what conditions (e.g., bail and monitoring) to impose if released
- Goal: avoid predispositional incarceration while preserving public safety
- Judges are required to consider three risk factors along with others
  - ① arrestee may fail to appear in court (FTA)
  - ② arrestee may engage in new criminal activity (NCA)
  - ③ arrestee may engage in new violent criminal activity (NVCA)
- **PSA** as an algorithmic recommendation to judges
  - classifying arrestees according to FTA and NCA/NVCA risks
  - derived from an application of a machine learning algorithm to a training data set based on past observations
  - different from COMPAS score

# A Field Experiment for Evaluating the PSA

- Dane County, Wisconsin
- PSA = weighted indices of ten factors
  - age as the single demographic factor: no gender or race
  - nine factors drawn from criminal history (prior convictions and FTA)
- PSA scores and recommendation
  - 1 two separate ordinal six-point risk scores for FTA and NCA
  - 2 one binary risk score for new violent criminal activity (NVCA)
  - 3 aggregate recommendation: signature bond, small and large cash bond
- Judges may have other information about an arrestee
  - affidavit by a police officer about the arrest
  - defense attorney may inform about the arrestee's connections to the community (e.g., family, employment)
- Field experiment
  - clerk assigns case numbers sequentially as cases enter the system
  - PSA is calculated for each case using a computer system
  - if the first digit of case number is even, PSA is given to the judge
  - mid-2017 – 2019 (randomization), 2-year follow-up for half sample



**DANE COUNTY CLERK OF COURTS**  
**Public Safety Assessment – Report**

215 S Hamilton St #1000  
Madison, WI 53703  
Phone: (608) 266-4311

Name: [REDACTED]

Spillman Name Number: [REDACTED]

DOB: [REDACTED]

Gender: Male

Arrest Date: 03/25/2017

PSA Completion Date: 03/27/2017

**New Violent Criminal Activity Flag**

No

**New Criminal Activity Scale**

1	2	3	4	5	6
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**Failure to Appear Scale**

1	2	3	4	5	6
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**Charge(s):**

961.41(1)(D)(1) MFC DELIVER HEROIN <3 GMS F 3

**Risk Factors:**

**Responses:**

- |  |             |
|--|-------------|
| 1. Age at Current Arrest                               | 23 or Older |
| 2. Current Violent Offense                             | No          |
| a. Current Violent Offense & 20 Years Old or Younger   | No          |
| 3. Pending Charge at the Time of the Offense           | No          |
| 4. Prior Misdemeanor Conviction                        | Yes         |
| 5. Prior Felony Conviction                             | Yes         |
| a. Prior Conviction                                    | Yes         |
| 6. Prior Violent Conviction                            | 2           |
| 7. Prior Failure to Appear Pretrial in Past 2 Years    | 0           |
| 8. Prior Failure to Appear Pretrial Older than 2 Years | Yes         |
| 9. Prior Sentence to Incarceration                     | Yes         |

**Recommendations:**

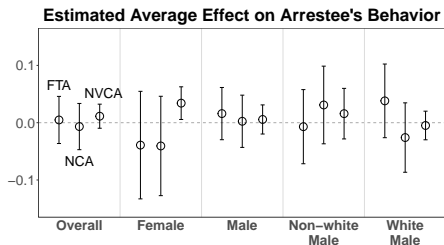
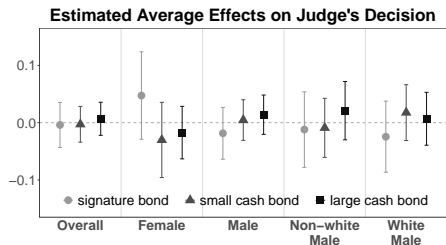
**Release Recommendation** - Signature bond

**Conditions** - Report to and comply with pretrial supervision

## PSA Provision, Demographics, and Outcomes

	no PSA			PSA			Total (%)
	Signature bond	Cash bond <i>small large</i>		Signature bond	Cash bond <i>small large</i>		
Non-white female	64	11	6	67	6	0	154 (8)
White female	91	17	7	104	17	10	246 (13)
Non-white male	261	56	49	258	53	57	734 (39)
White male	289	48	44	276	54	46	757 (40)
FTA committed	218	42	16	221	45	16	558 (29)
<i>not</i> committed	487	90	90	484	85	97	1333 (71)
NCA committed	211	39	14	202	40	17	523 (28)
<i>not</i> committed	494	93	92	503	90	96	1368 (72)
NVCA committed	36	10	3	44	10	6	109 (6)
<i>not</i> committed	669	122	103	661	120	107	1782 (94)
Total (%)	705 (37)	132 (7)	106 (6)	705 (37)	130 (7)	113 (6)	1891 (100)

# Intention-to-Treat Analysis of PSA Provision



- Insignificant average effects on a judge's decisions and arrestee's behavior
- Does PSA provision help a judge make better decisions?
- Good decision: detain risky arrestees, release safe arrestees
- Need to explore causal heterogeneity based on **risk-levels**

# The Setup of the Proposed Methodology (Binary Decision)

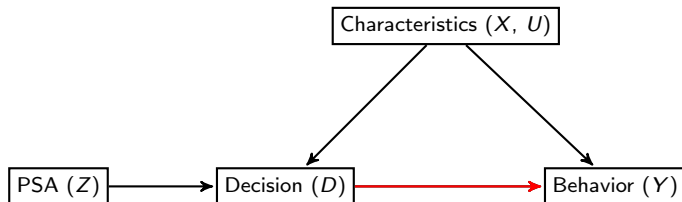
- Notation

- $Z_i$ : PSA provision indicator
- $D_i$ : detain ( $D_i = 1$ ) or release ( $D_i = 0$ )
- $Y_i$ : binary outcome (e.g., NCA)
- $X_i$ : observed covariates
- $U_i$ : unobserved covariates

- Potential outcomes

- $D_i(z)$ : potential value of the decision when  $Z_i = z$
- $Y_i(z, d)$ : potential outcome when  $Z_i = z$  and  $D_i = d$
- No interference across cases: first arrests only

# Assumptions



- **Randomized treatment assignment:**  $\{D_i(z), Y_i(z, d), X_i, U_i\} \perp\!\!\!\perp Z_i$
- **Exclusion restriction:**  $Y_i(z, d) = Y_i(d)$
- **Monotonicity:**  $Y_i(0) \geq Y_i(1)$

# Causal Quantities of Interest

- Principal stratification (Frangakis and Rubin 2002)
  - $(Y_i(1), Y_i(0)) = (0, 1)$ : preventable cases
  - $(Y_i(1), Y_i(0)) = (1, 1)$ : risky cases
  - $(Y_i(1), Y_i(0)) = (0, 0)$ : safe cases
  - $(Y_i(1), Y_i(0)) = (1, 0)$ : eliminated by monotonicity

- Average principal causal effects of PSA on judges' decisions:

$$\text{APCE}_p = \mathbb{E}\{D_i(1) - D_i(0) \mid Y_i(1) = 0, Y_i(0) = 1\},$$

$$\text{APCE}_r = \mathbb{E}\{D_i(1) - D_i(0) \mid Y_i(1) = 1, Y_i(0) = 1\},$$

$$\text{APCE}_s = \mathbb{E}\{D_i(1) - D_i(0) \mid Y_i(1) = 0, Y_i(0) = 0\}.$$

- If PSA is helpful, we should have  $\text{APCE}_p > 0$  and  $\text{APCE}_s < 0$ .
- The desirable sign of  $\text{APCE}_r$  depends on various factors.



## Partial Identification

- The assumptions of randomization, exclusion restriction, and monotonicity imply,

$$\text{APCEp} = \frac{\Pr(Y_i = 1 \mid Z_i = 0) - \Pr(Y_i = 1 \mid Z_i = 1)}{\Pr\{Y_i(0) = 1\} - \Pr\{Y_i(1) = 1\}}$$

$$\text{APCEr} = \frac{\Pr(D_i = 1, Y_i = 1 \mid Z_i = 1) - \Pr(D_i = 1, Y_i = 1 \mid Z_i = 0)}{\Pr\{Y_i(1) = 1\}}$$

$$\text{APCEs} = \frac{\Pr(D_i = 0, Y_i = 0 \mid Z_i = 0) - \Pr(D_i = 0, Y_i = 0 \mid Z_i = 1)}{1 - \Pr\{Y_i(0) = 1\}}$$

- The signs of APCE are identifiable
- The bounds on APCE can be obtained

$$\begin{aligned} \Pr\{Y_i(d) = 1\} &= \Pr\{Y_i = 1 \mid D_i = d\} \Pr(D_i = d) \\ &\quad + \Pr\{Y_i(d) = 1 \mid D_i = 1 - d\} \Pr(D_i = 1 - d) \end{aligned}$$

# Point Identification

- **Unconfoundedness:**  $Y_i(d) \perp\!\!\!\perp D_i \mid X_i, Z_i = z$
- Violation of unconfoundedness
  - unobserved covariates between decision and outcome
  - sensitivity analysis
- **Principal score**

$$e_P(x) = \Pr\{Y_i(1) = 0, Y_i(0) = 1 \mid X_i = x\} = 1 - e_R(x) - e_S(x)$$

$$e_R(x) = \Pr\{Y_i(1) = 1, Y_i(0) = 1 \mid X_i = x\} = \Pr(Y_i = 1 \mid D_i = 1, X_i = x)$$

$$e_S(x) = \Pr\{Y_i(1) = 0, Y_i(0) = 0 \mid X_i = x\} = \Pr(Y_i = 0 \mid D_i = 0, X_i = x)$$

- Identification formula

$$\text{APCEp} = \mathbb{E}\left[\underbrace{\frac{e_P(x)}{\mathbb{E}\{e_P(X_i)\}}}_{\text{weight}} D_i \mid Z_i = 1\right] - \mathbb{E}\left[\underbrace{\frac{e_P(x)}{\mathbb{E}\{e_P(X_i)\}}}_{\text{weight}} D_i \mid Z_i = 0\right]$$

an analogous formula applies to risky and safe groups

## Extension to Ordinal Decision

- Judges decisions are typically ordinal (e.g., bail amount)
  - $D_i = 0, 1, \dots, k$ : a bail of increasing amount
  - Monotonicity**:  $Y_i(d_1) \geq Y_i(d_2)$  for  $d_1 \leq d_2$
- Principal strata based on an ordinal measure of risk

$$R_i = \begin{cases} \min\{d : Y_i(d) = 0\} & \text{if } Y_i(k) = 0 \\ k + 1 & \text{if } Y_i(k) = 1 \end{cases}$$

- Least amount of bail that keeps an arrestee from committing NCA
- Example with  $k = 2$

principal strata	$(Y_i(0), Y_i(1), Y_i(2))$	$R_i$
risky cases	$(1, 1, 1)$	3
preventable cases	$(1, 1, 0)$	2
easily preventable cases	$(1, 0, 0)$	1
safe cases	$(0, 0, 0)$	0

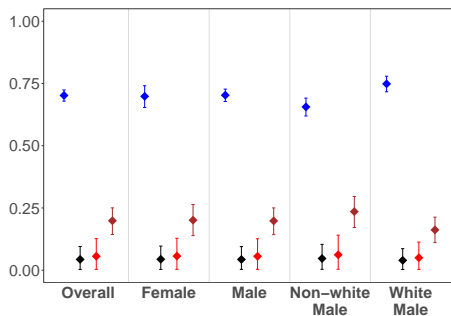
# APCE for Ordinal Decision

- For people with  $R_i = r$ 
  - judges make decision  $D_i \geq r \rightsquigarrow$  not commit a crime
  - judges make decision  $D_i < r \rightsquigarrow$  commit a crime
- **Causal quantities of interest** : reduction in the proportion of NCA attributable to PSA provision

$$\text{APCEp}(r) = \Pr\{D_i(1) \geq r \mid R_i = r\} - \Pr\{D_i(0) \geq r \mid R_i = r\}$$

- Nonparametric identification under unconfoundedness
- Empirical results presented below are based on parametric modeling

# Empirical Results: New Criminal Activity

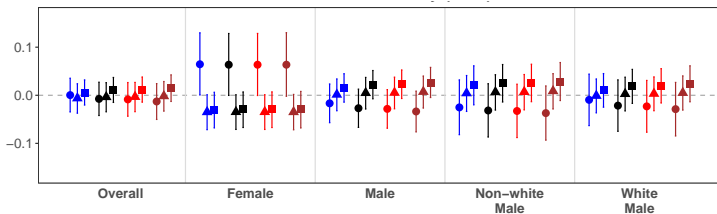


safe

easily preventable

preventable

risky



● signature bond ▲ small cash bond ■ large cash bond

# Measuring and Estimating the Degree of Fairness

- How fair are the judge's decisions?
- Between-group deviation in decision probability within each principal stratum

$$\Delta_r(z) = \max_{a, a', d} |\Pr\{D_i(z) \geq d \mid A_i = a, R_i = r\} \\ - \Pr\{D_i(z) \geq d \mid A_i = a', R_i = r\}|$$

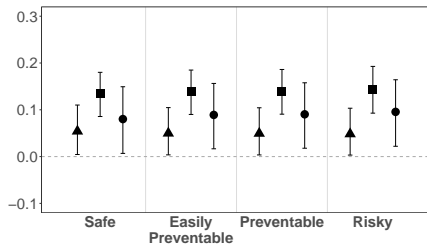
for  $1 \leq d \leq k$  and  $0 \leq r \leq k + 1$

- Does the provision of PSA improve the fairness of the judge's decision?

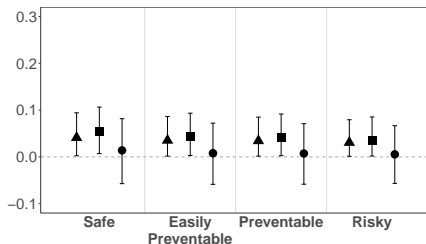
$$\Delta_r(1) - \Delta_r(0)$$

# Gender and Racial Fairness

(a) Gender fairness



(b) Racial fairness



$\blacktriangle$ :  $\Delta_r(0)$  without PSA

$\blacksquare$ :  $\Delta_r(1)$  with PSA

$\bullet$ :  $\Delta_r(1) - \Delta_r(0)$

# Concluding Remarks

- Fairness of human and algorithmic decision-making needs to be placed in the causal inference framework
- We must consider how the decision affects individuals
- Principal fairness: replace observed outcomes with potential outcomes
- Challenge: causal inference requires counterfactual
- Point identification requires untestable assumptions
- Papers: <https://imai.fas.harvard.edu/research>
  - Imai, K. and Jiang, Z. (2023). "Principal fairness for human and algorithmic decision-making." *Statistical Science*
  - Imai, K., Z. Jiang, D. J. Greiner, et al. (2023). "Experimental Evaluation of Algorithm-Assisted Human Decision-Making: Application to Pretrial Public Safety Assessment." (with discussion) *Journal of the Royal Statistical Society, Series A (Statistics in Society)*